

ECE 340 Lectures 40

Semiconductor Electronics

Spring 2022

10:00-10:50am

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Today's Discussion

- **Analytical model of the Bipolar Junction Transistor (BJT)**
- **Transistor as amplifier**

BJT results so far

$$\gamma = \frac{i_{Ep}}{i_E} = \frac{i_{Ep}}{i_{Ep} + i_{En}}$$

**emitter injection
efficiency**

$$i_C = B i_{Ep}$$

base transport factor

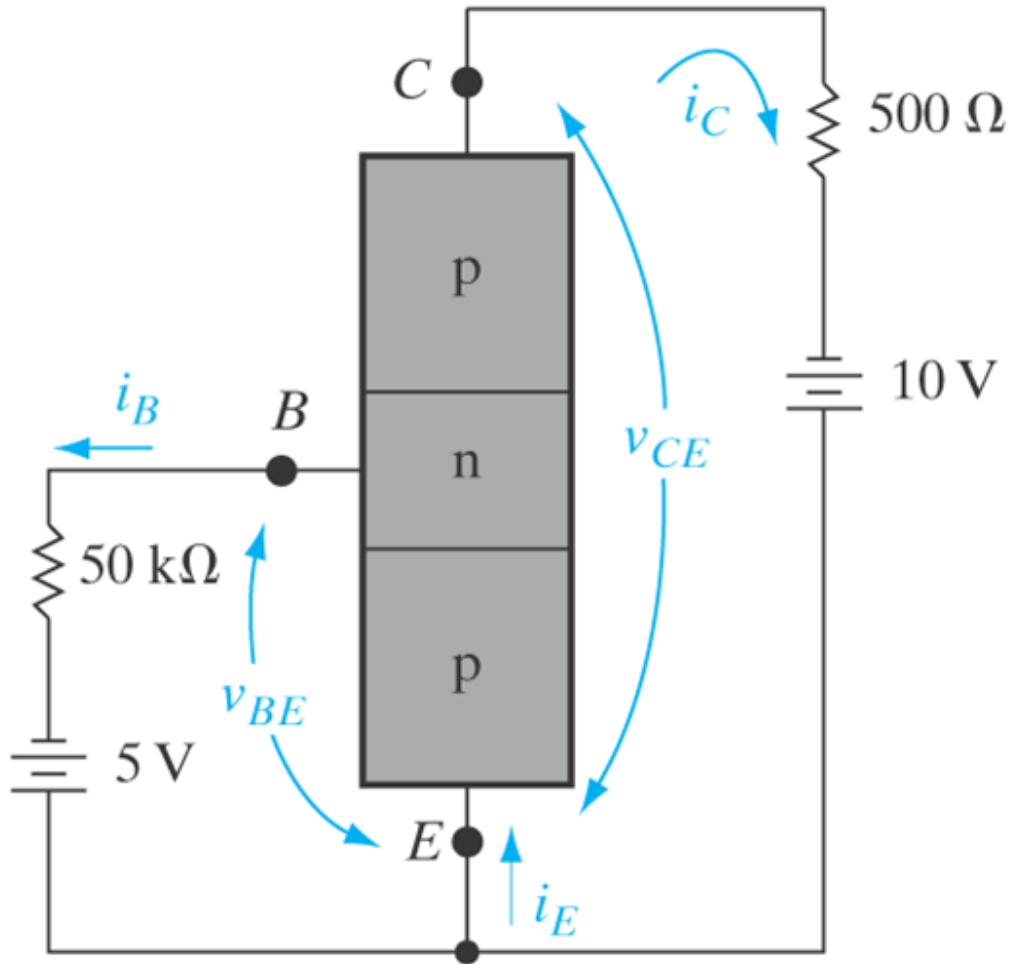
$$\frac{i_C}{i_E} = B\gamma = \alpha$$

**current transfer
ratio**

$$\frac{i_C}{i_B} = \frac{\alpha}{1 - \alpha} = \beta$$

amplification factor

Example



Base recombination time

$$\tau_n = \tau_p = 10 \mu\text{s}$$

Base transit time

$$\tau_t = 0.1 \mu\text{s}$$

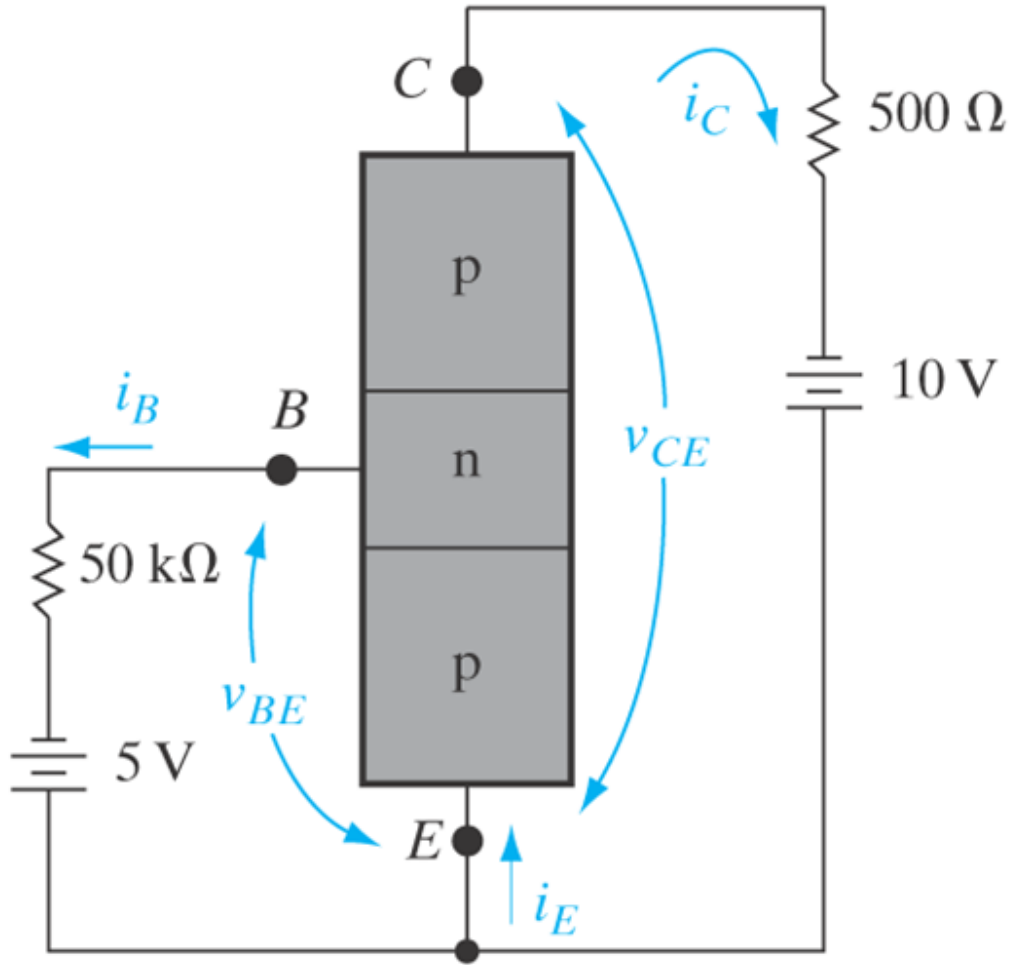
Amplification factor

$$\beta = \frac{i_C}{i_B} = \frac{\tau_n}{\tau_t} = 100$$

Current Transfer ratio

$$\alpha = \frac{\beta}{1 + \beta} = \frac{100}{101} = 0.99$$

Example



Amplification factor

$$\beta = 100$$

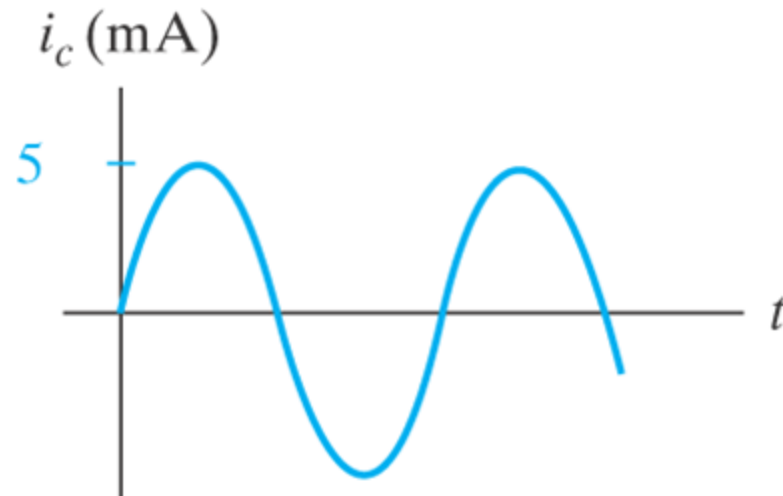
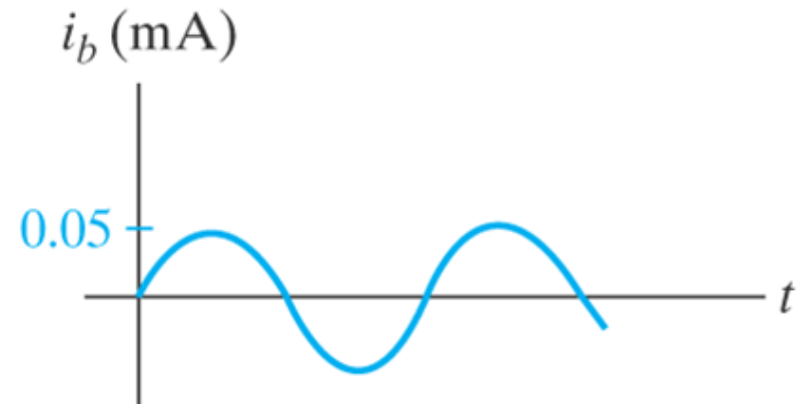
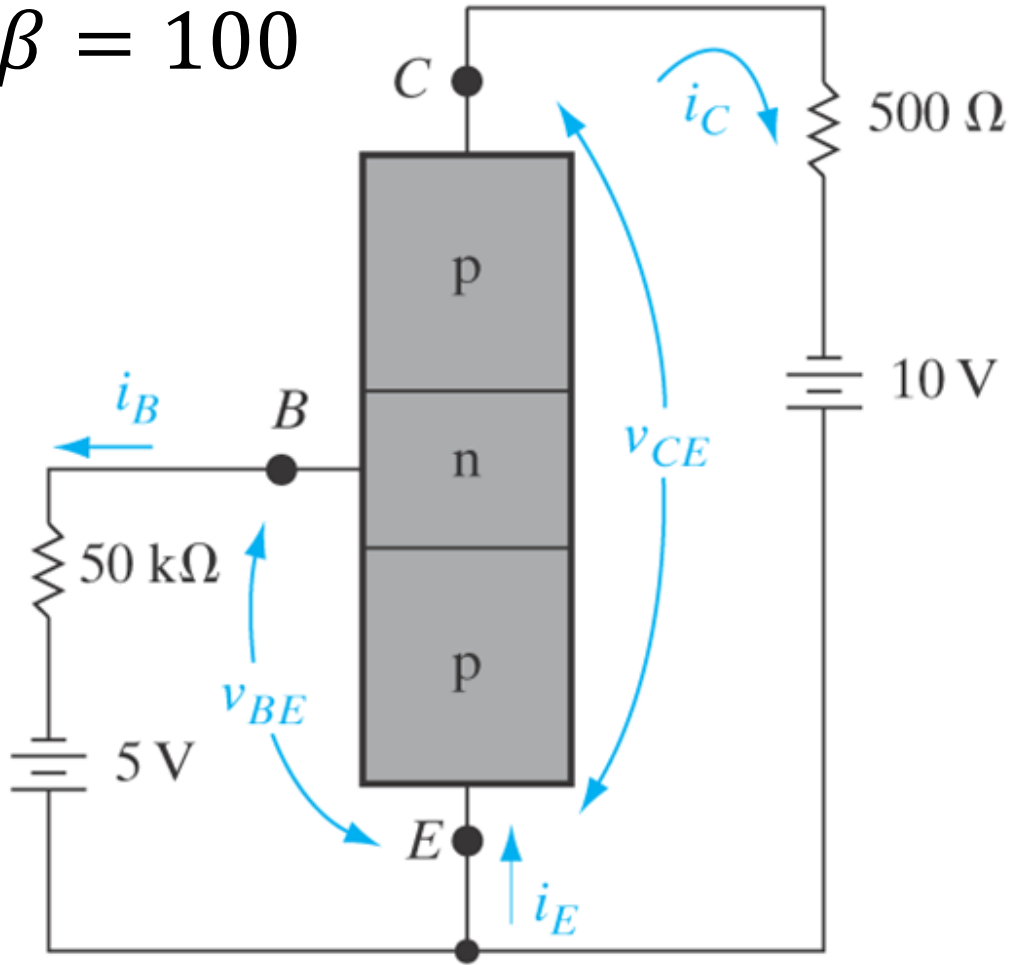
Assume $v_{BE} \approx 0$

$$I_B = \frac{5V}{50k\Omega} = 0.1 \text{ mA}$$

$$I_C = \beta I_B = 10 \text{ mA}$$

Example

$$\beta = 100$$



For the curious ones:

- Video by Bill Hammack on the first transistor invented by Bardeen and Brattain at Bell Labs (point-contact transistor)

<https://www.youtube.com/watch?v=RdYHljZi7ys>

The book by Shockley contains an extensive description of the point-contact transistor, based on metal-semiconductor junctions rather than p-n junctions

<https://archive.org/details/ElectronsAndHolesInSemiconductors>

- AT&T Archives video: Genesis of the Transistor:

<https://www.youtube.com/watch?v=WiQvGRjrLnU>

Mathematical analysis of the $p-n-p$ BJT

- **Some simplifying assumptions are necessary in order to develop a manageable model which is general and valid for general bias conditions:**
 1. **Negligible drift in the base region (holes move by diffusion)**
 2. **Emitter injection efficiency $\gamma = 1$ (emitter is highly doped $p+$)**
 3. **Reverse saturation current at the collector is negligible**
 4. **Uniform cross-sectional area A (1-D model)**
 5. **Steady-state conditions**

Posted handout on NBD and BJT:

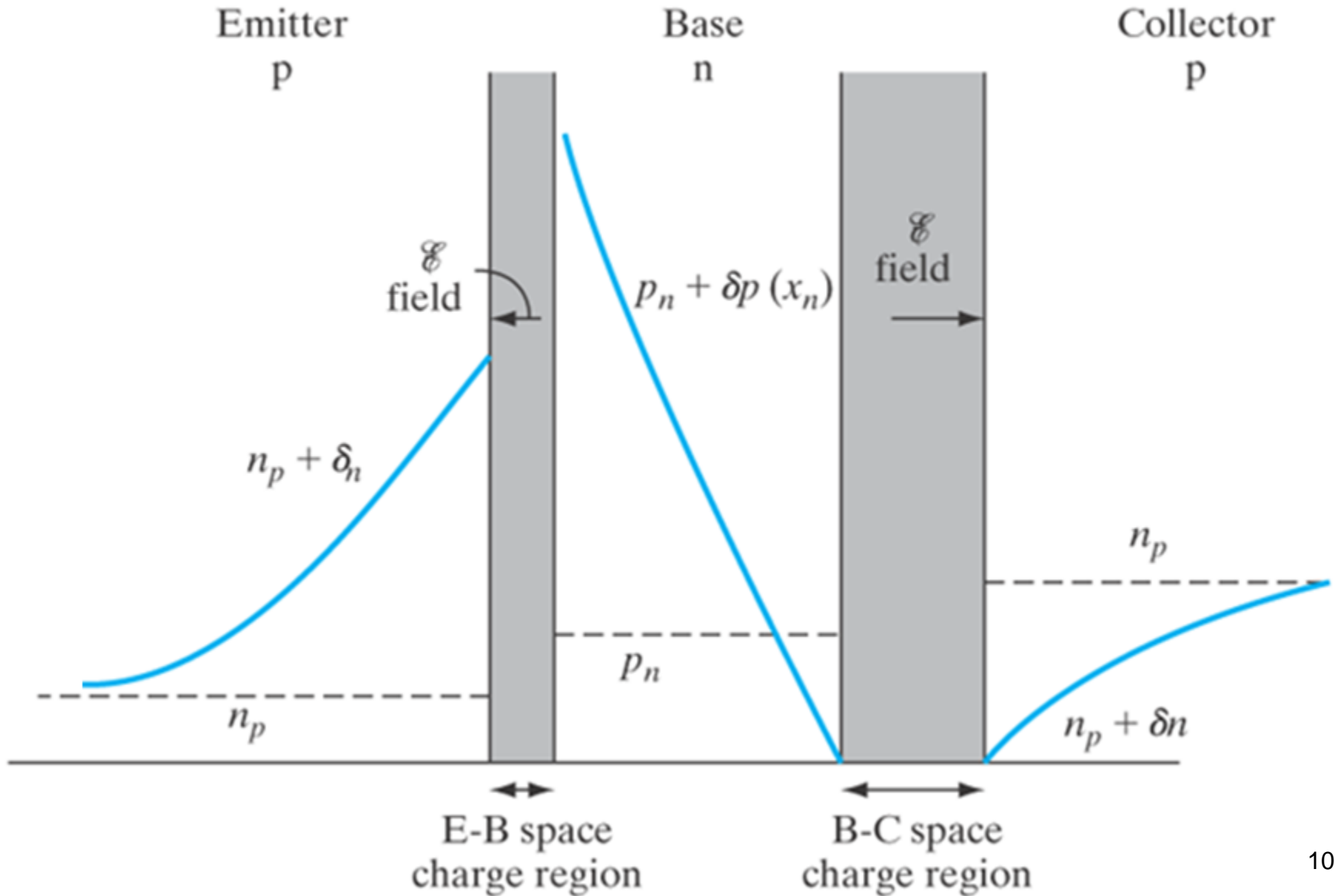
We are going to focus on the significance of the results and on physical understanding of physical behavior.

Details of the analytical solution for the 1-D model BJT are outlined in the posted handout and are left as optional reading for the interested students.

Actual complete simulations of realistic devices are carried out by numerical solution of the **coupled system of semiconductor equations** consisting of:

- continuity equations for electrons and holes based on the drift-diffusion current model
- Poisson equation to obtain self-consistent space dependent electric fields

Excess carriers in the whole device



Results obtained from analytical solution

$$I_{Ep} = qA \frac{D_p}{L_p} \left[\Delta p_E \operatorname{ctnh} \frac{W_B}{L_p} - \Delta p_C \operatorname{csch} \frac{W_B}{L_p} \right]$$

$$I_C = qA \frac{D_p}{L_p} \left[\Delta p_E \operatorname{csch} \frac{W_B}{L_p} - \Delta p_C \operatorname{ctnh} \frac{W_B}{L_p} \right]$$

$$I_B = qA \frac{D_p}{L_p} \left[(\Delta p_E + \Delta p_C) \tanh \frac{W_B}{2L_p} \right]$$

For the narrow base diode

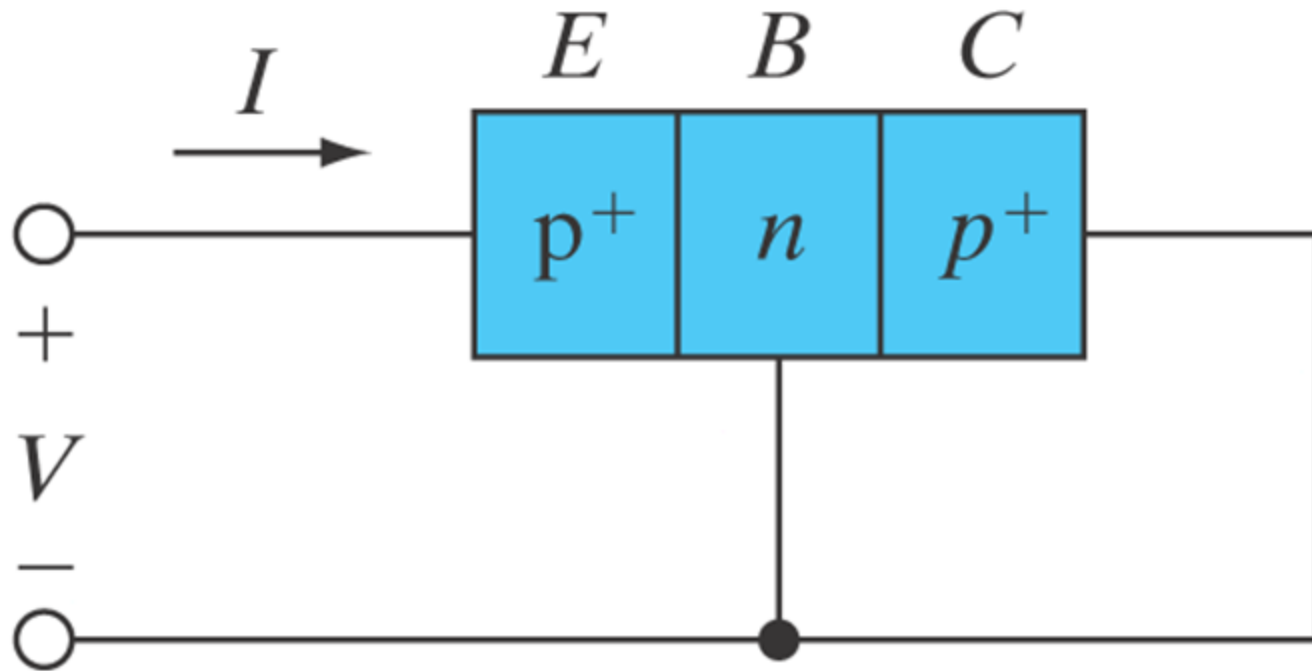
$$I_p(x_n = 0) = qA \frac{D_p}{L_p} \Delta p_n \operatorname{ctnh} \frac{\ell}{L_p}$$

$$I_p(x_n = \ell) = qA \frac{D_p}{L_p} \Delta p_n \operatorname{csch} \frac{\ell}{L_p}$$

$$I_n(\text{recomb}) = qA \frac{D_p}{L_p} \Delta p_n \tanh \frac{\ell}{2L_p}$$

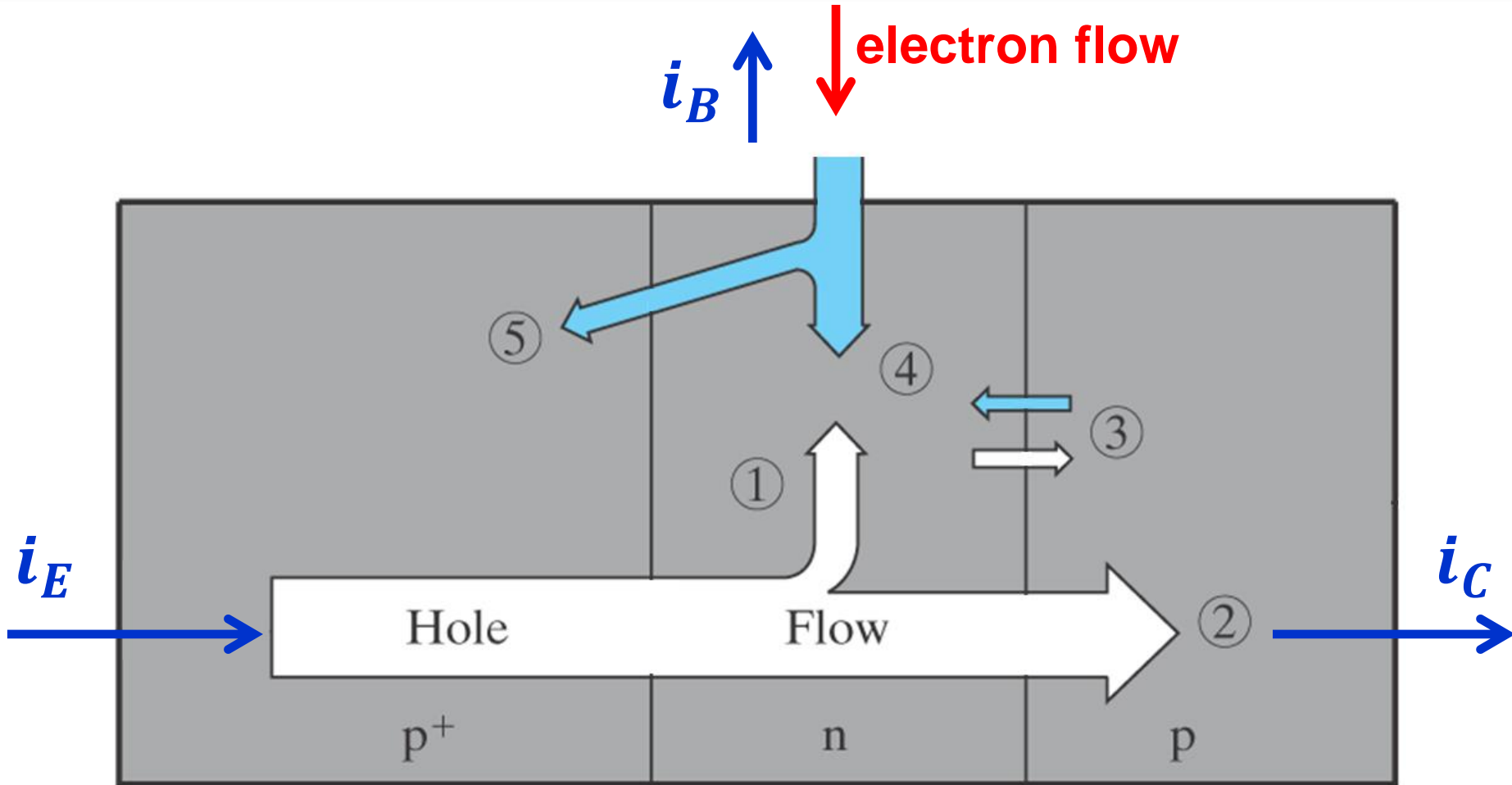
With $\Delta p_c \approx 0$ essentially the same result obtained for BJT

In fact, NBD is equivalent to this BJT



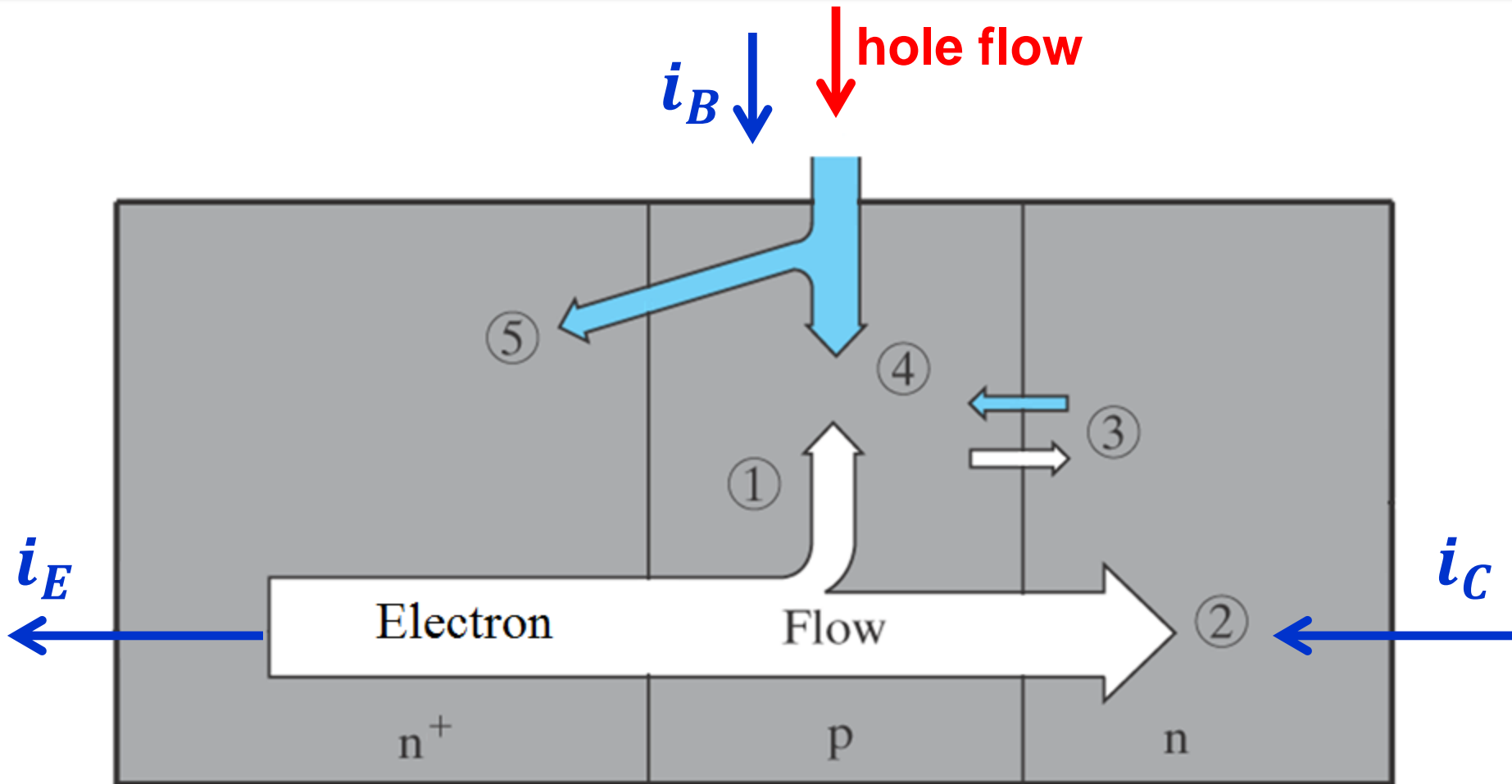
$$V_{CB} = 0 \quad \rightarrow \quad \Delta p_C = 0$$

Recall the carrier flow for p⁺-n-p



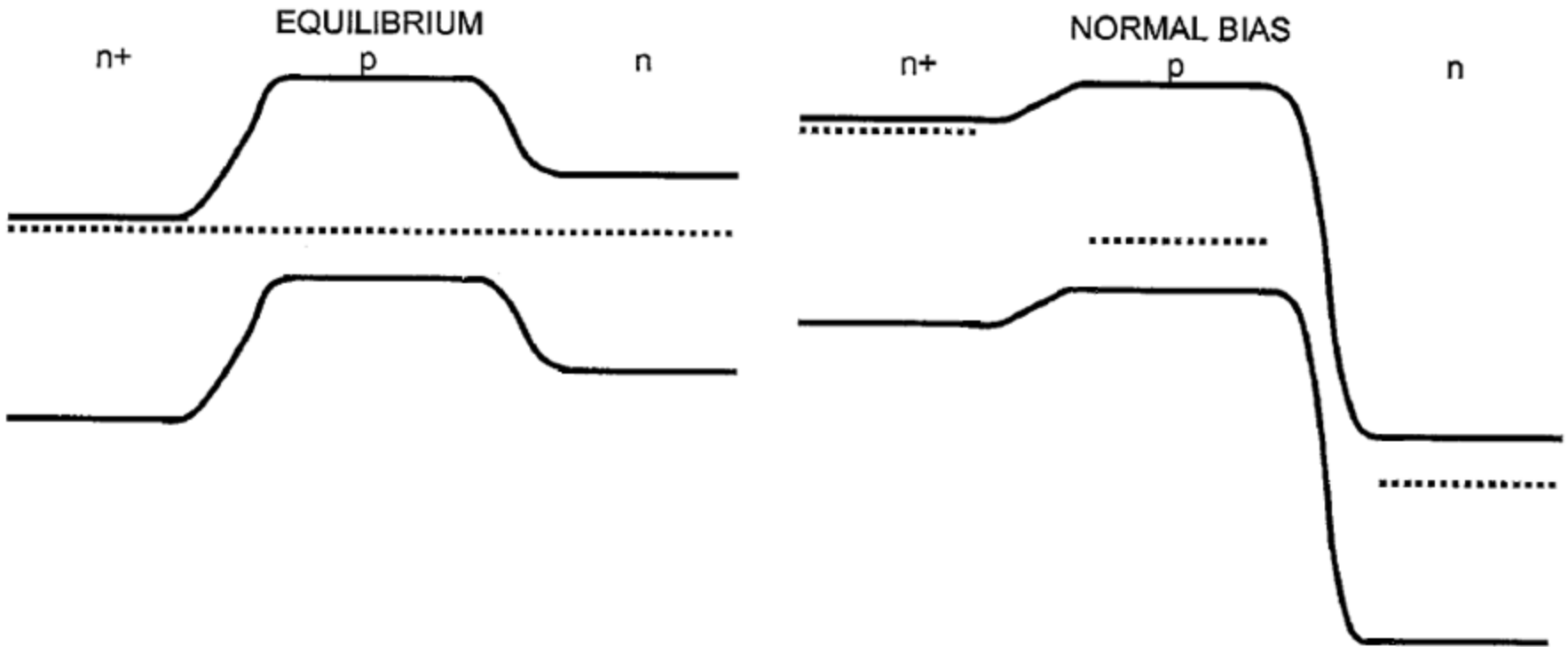
$$\xrightarrow{i_E} = \left\{ \begin{array}{l} \xrightarrow{i_{Ep}} \\ \xrightarrow{i_{En}} \end{array} \right. \quad \xrightarrow{i_C}$$

Redraw carrier flow for n⁺-p-n

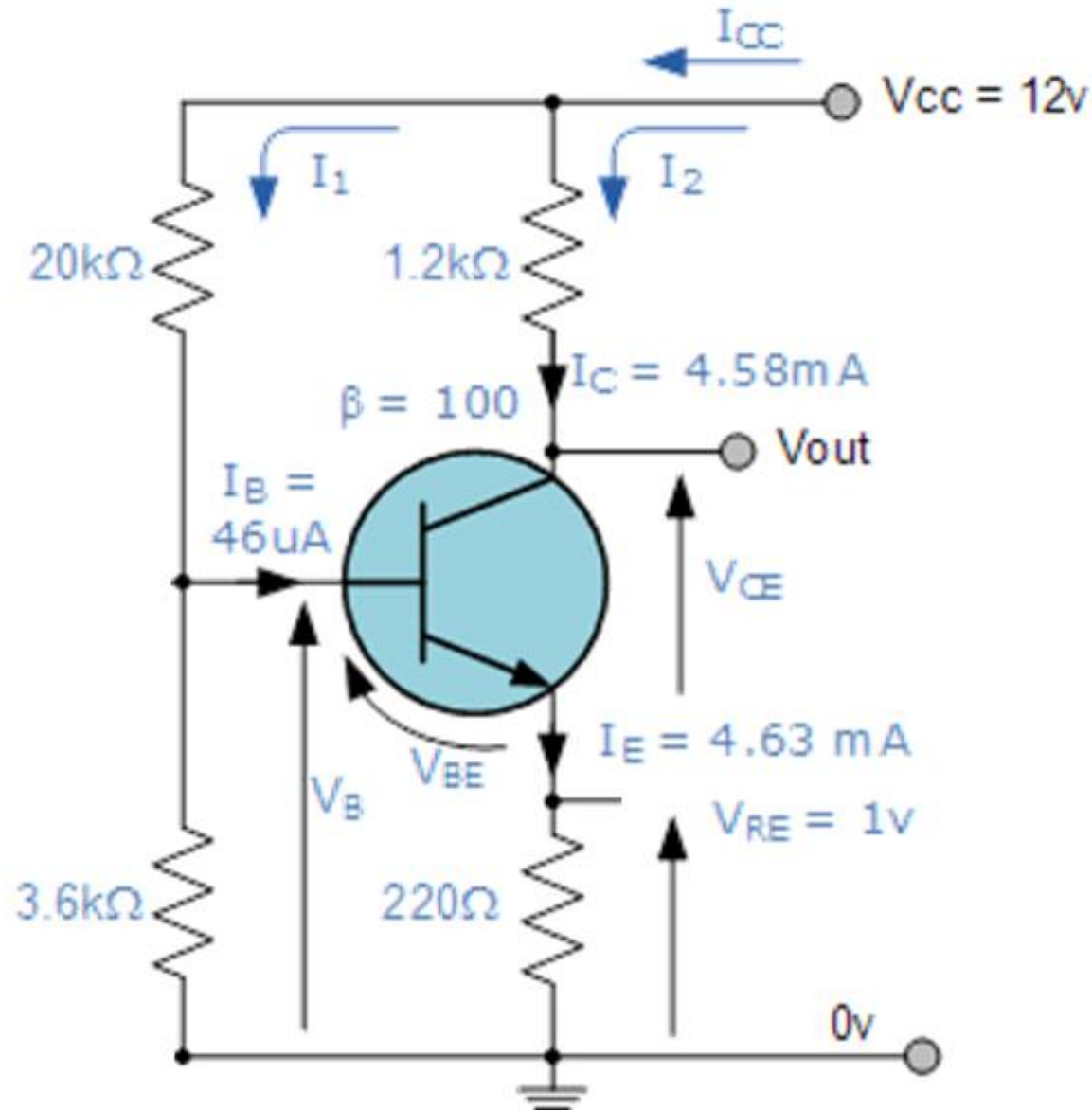


$$i_E = \left\{ \begin{array}{l} \leftarrow i_{En} \\ \leftarrow i_{Ep} \end{array} \right. \quad \leftarrow i_C$$

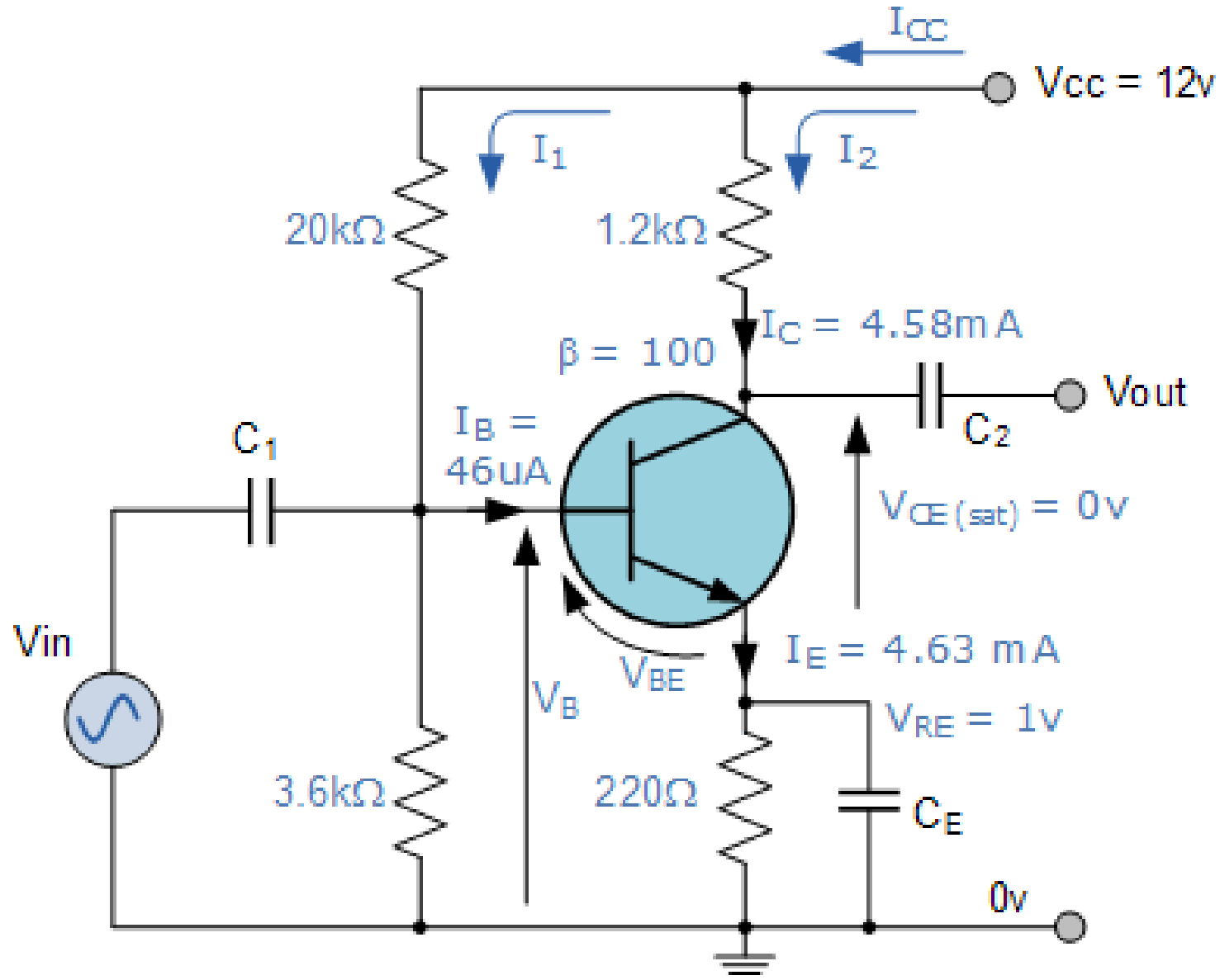
Redraw band diagram for n^+p-n



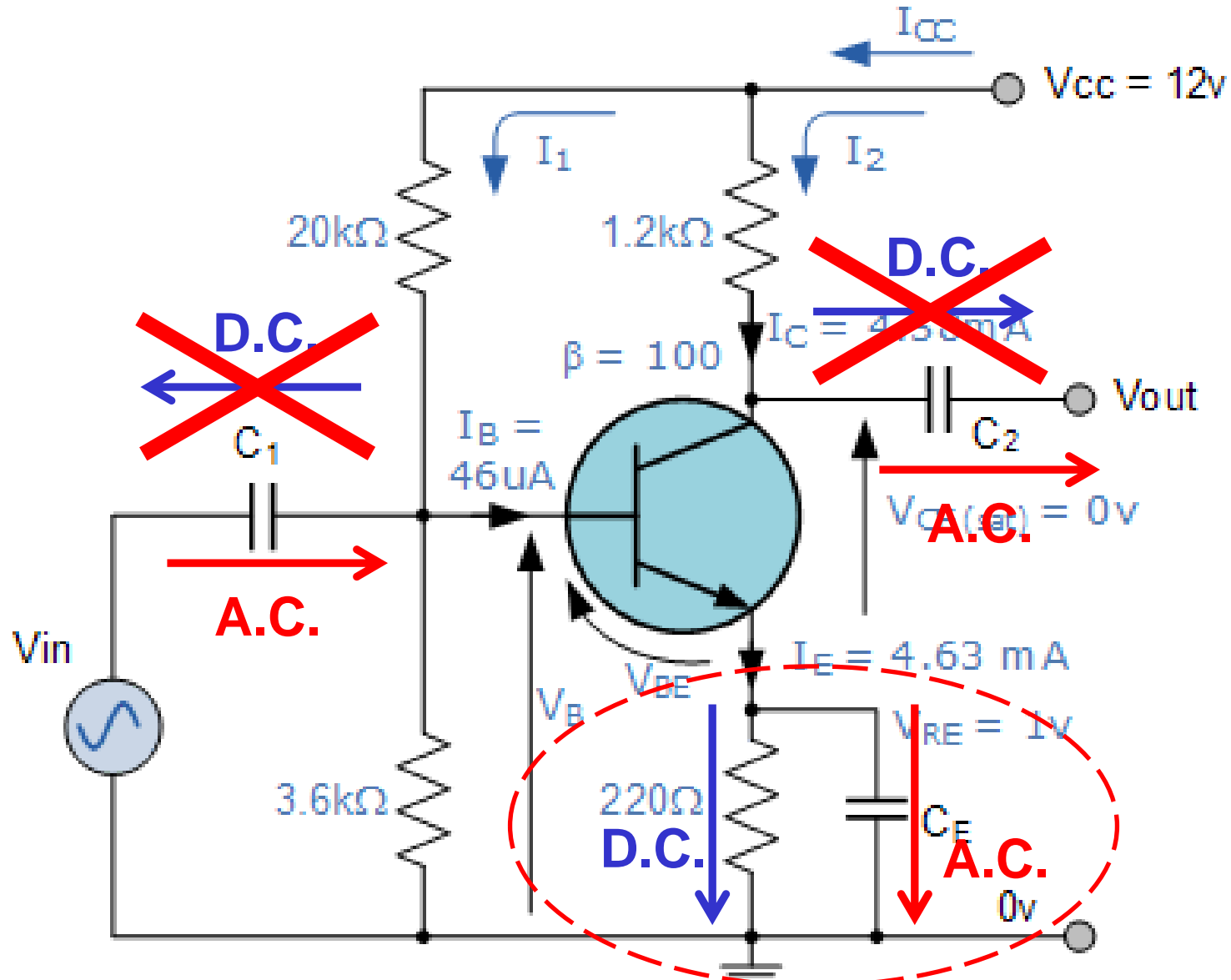
Single battery bias for n-p-n BJT



Amplifier stage based on n-p-n BJT

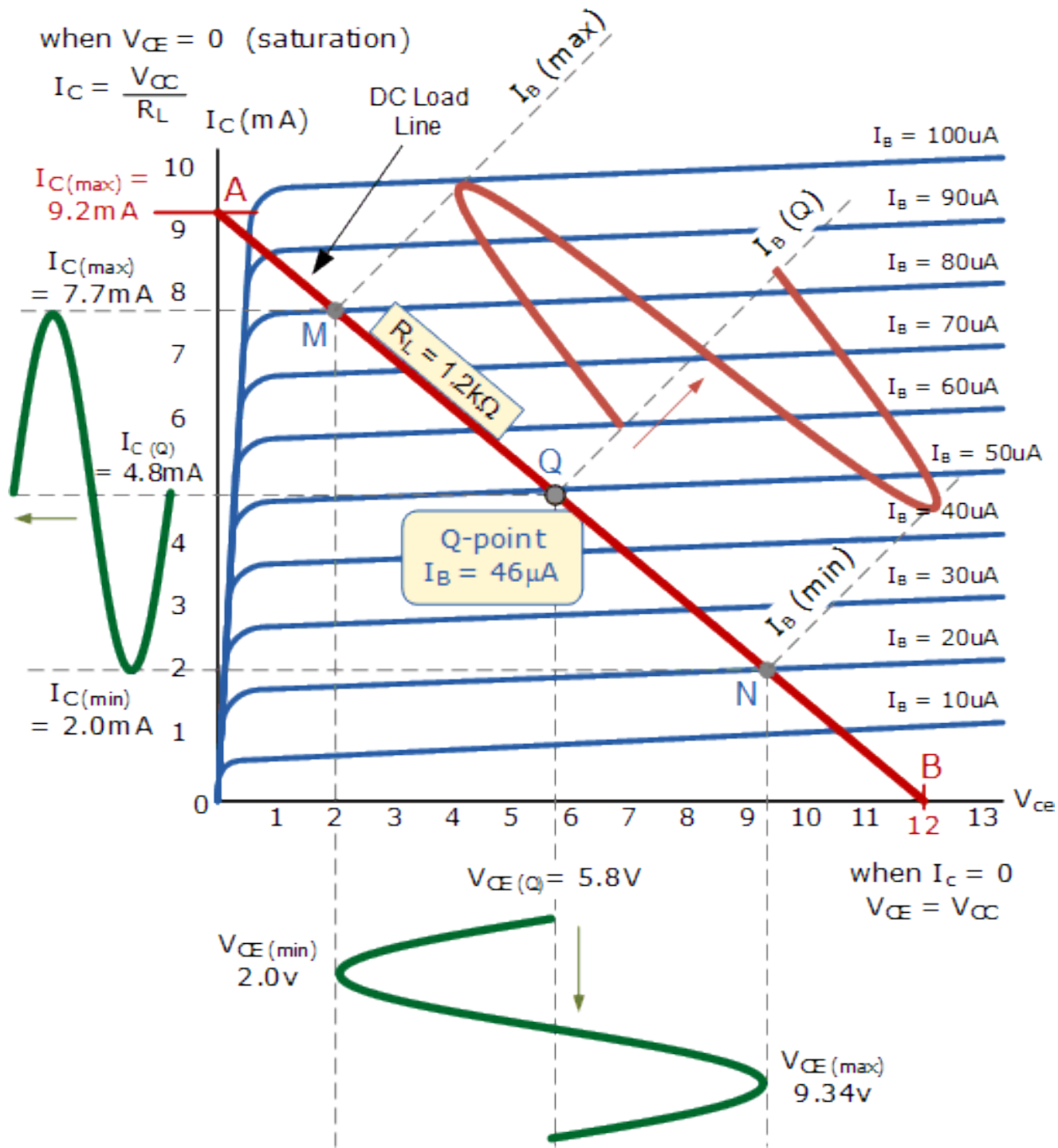


Amplifier stage based on n-p-n BJT

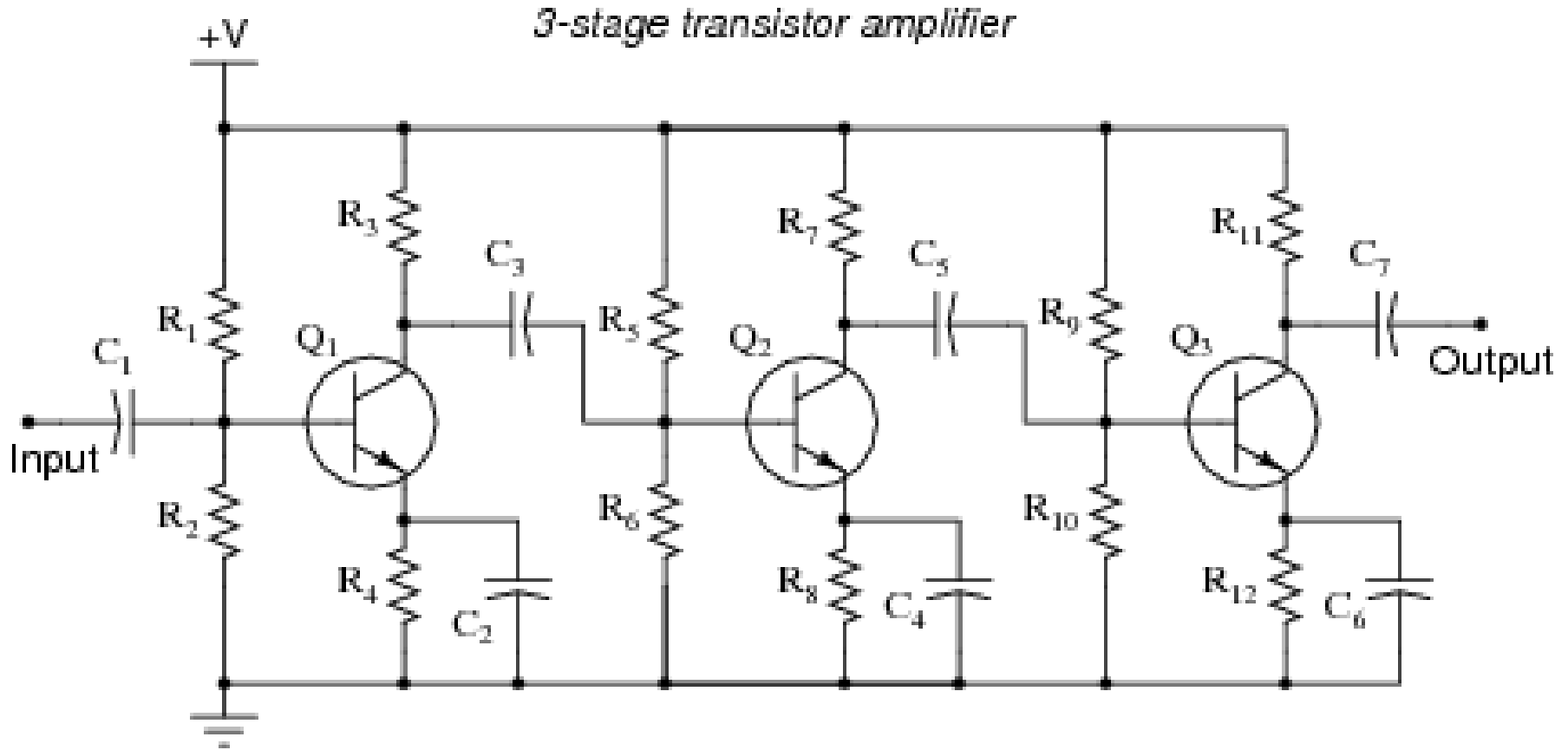


when $V_{CE} = 0$ (saturation)

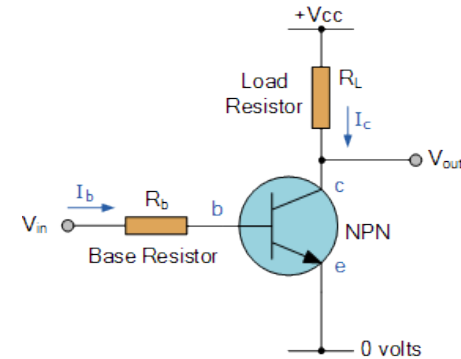
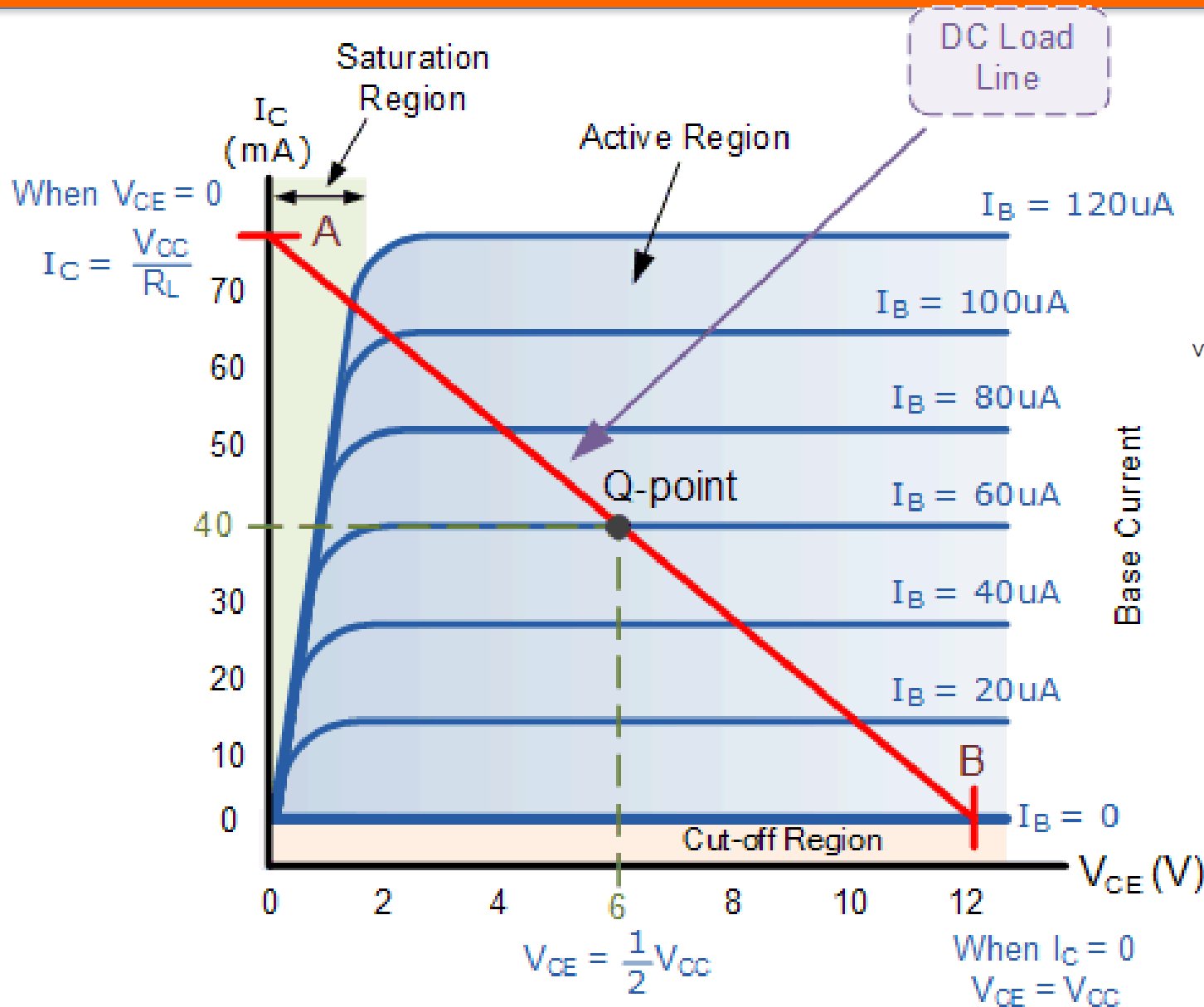
$$I_C = \frac{V_{CC}}{R_L}$$



Multi-stage amplifier example



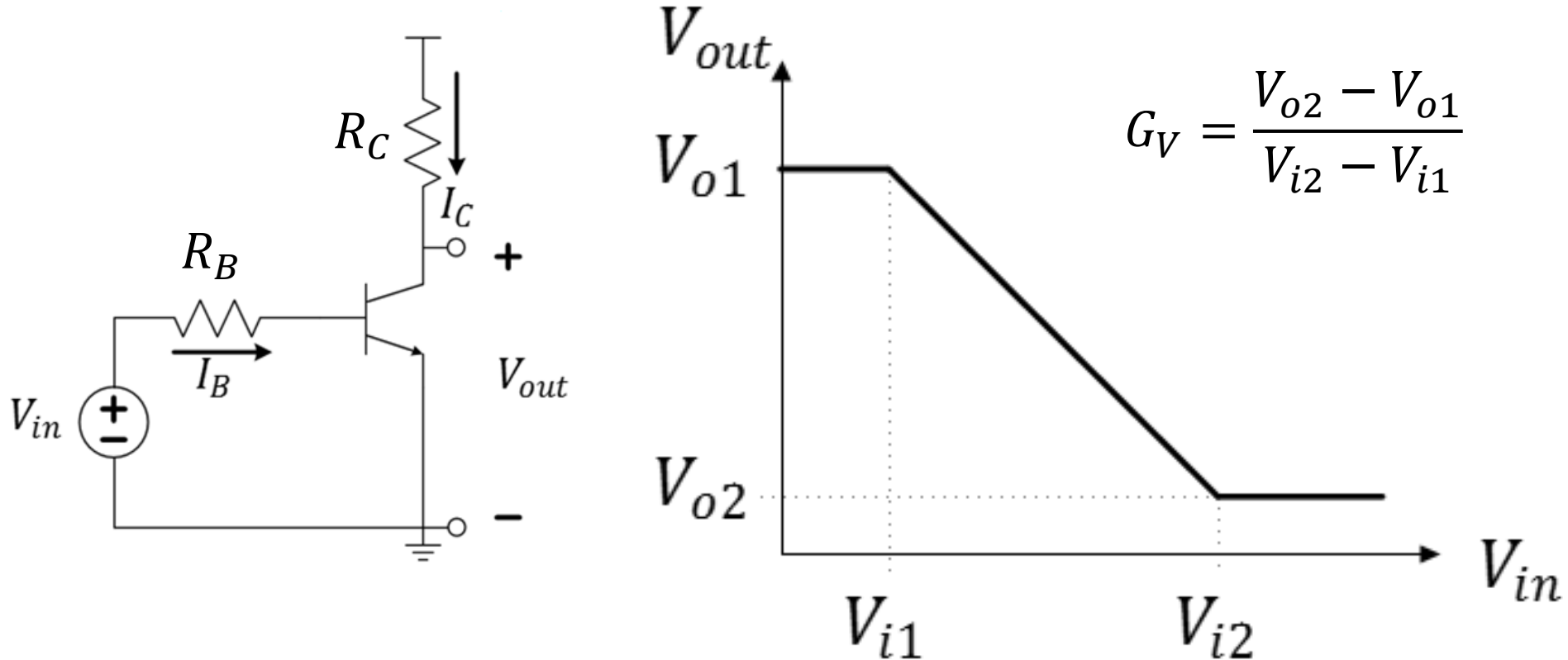
BJT as amplifier or as switch



**Q bias point
Amplifier**

**A and B points
Logic Inverter**

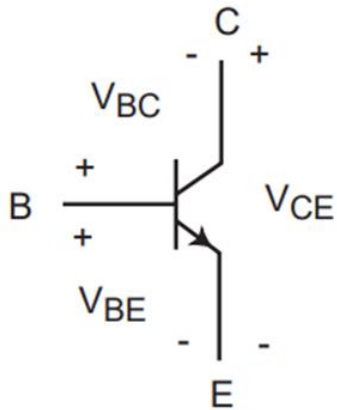
Voltage Transfer Characteristics



incremental voltage gain

$$G_V = \frac{\Delta V_{out}}{\Delta V_{in}} = \frac{-\Delta I_C R_C}{\Delta I_B R_B} = -\beta \frac{R_C}{R_B}$$

Summary of n-p-n BJT regimes



REVERSE ACTIVE

$$V_C < V_B < V_E$$

not useful

SATURATION

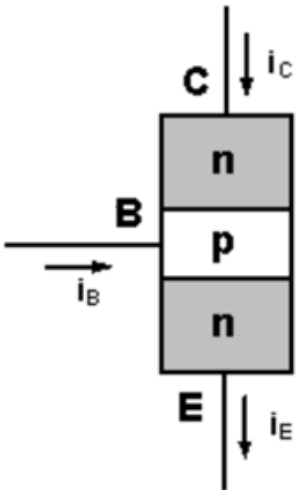
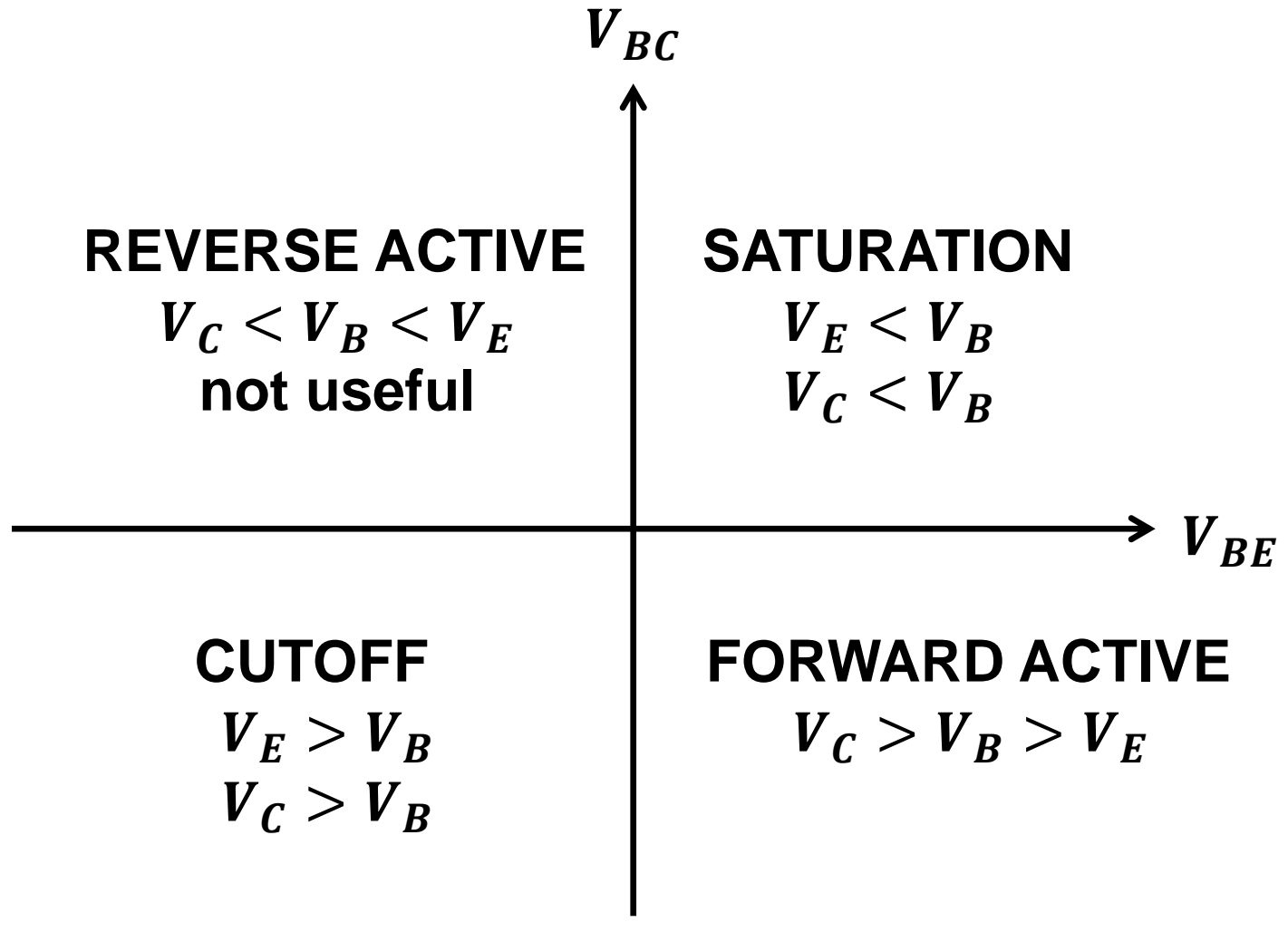
$$V_E < V_B$$
$$V_C < V_B$$

CUTOFF

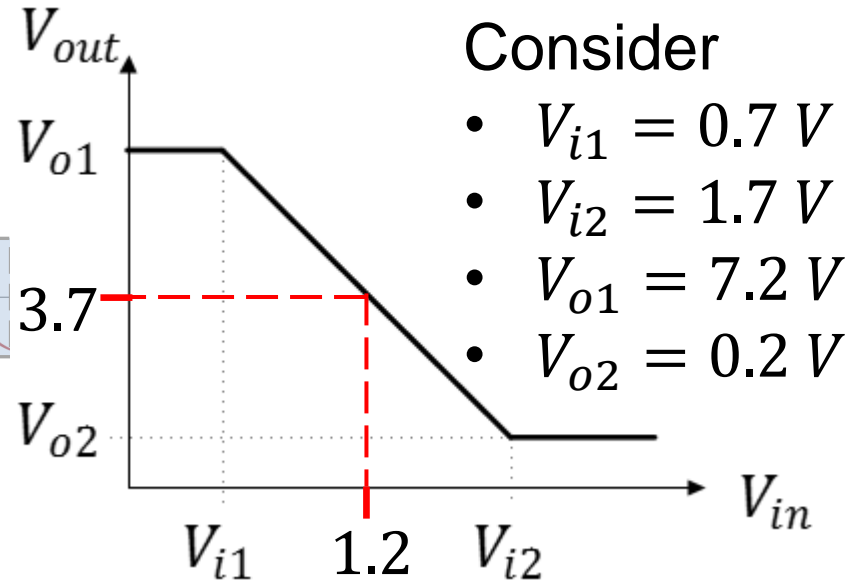
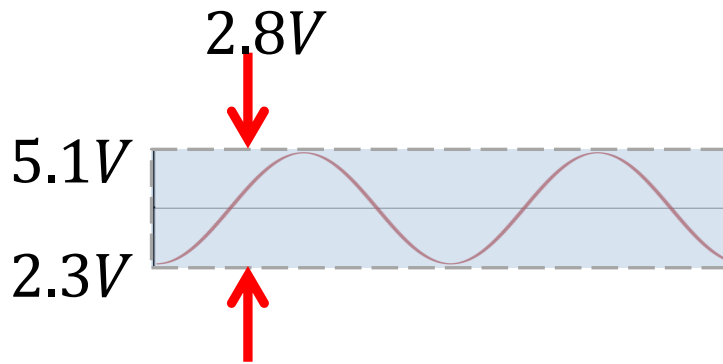
$$V_E > V_B$$
$$V_C > V_B$$

FORWARD ACTIVE

$$V_C > V_B > V_E$$



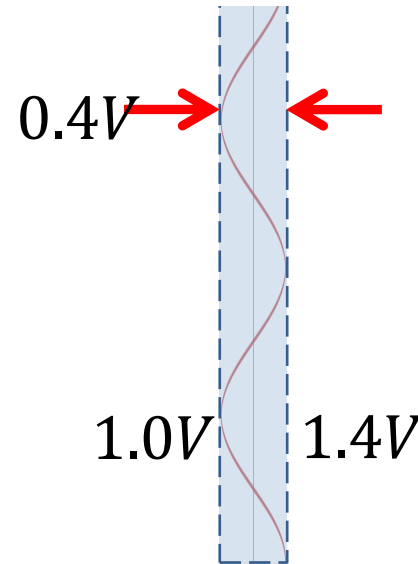
Amplification Example



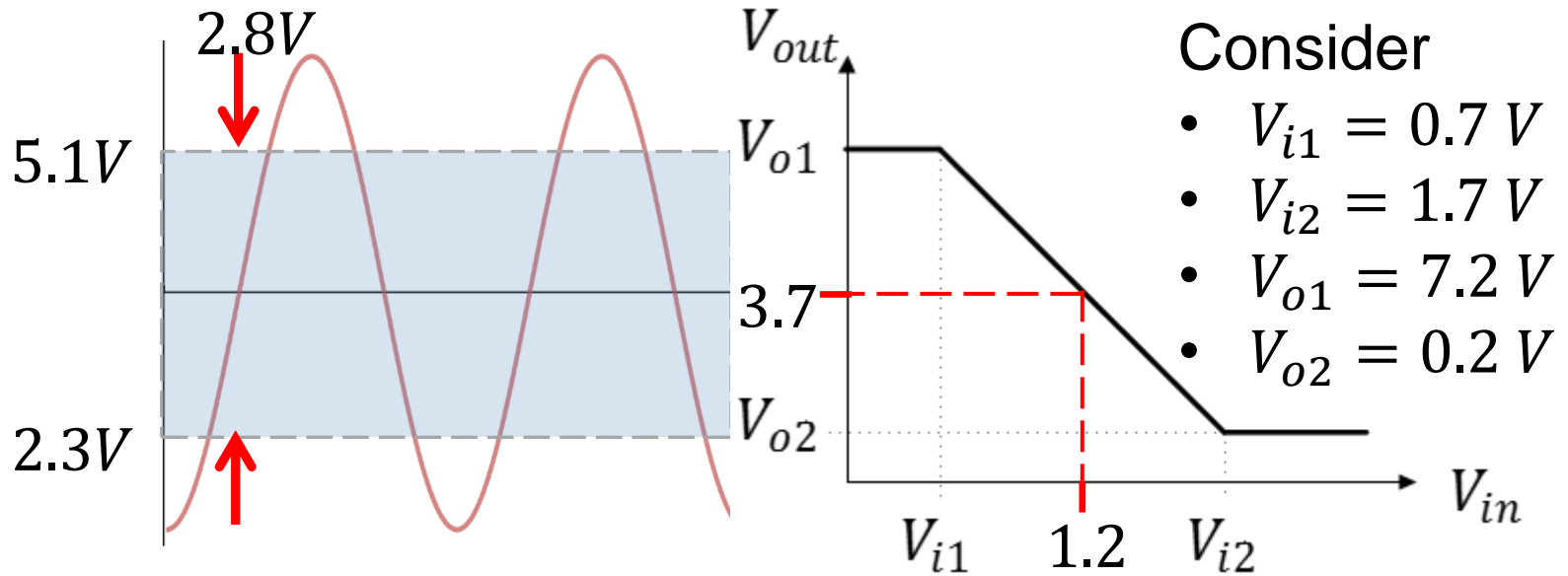
- Consider
- $V_{i1} = 0.7V$
 - $V_{i2} = 1.7V$
 - $V_{o1} = 7.2V$
 - $V_{o2} = 0.2V$

$$V_{IN} = 1.2 + 0.2\cos(2\pi 100t)$$

$$V_{OUT} = 3.7 - 1.4\cos(2\pi 100t)$$



Example

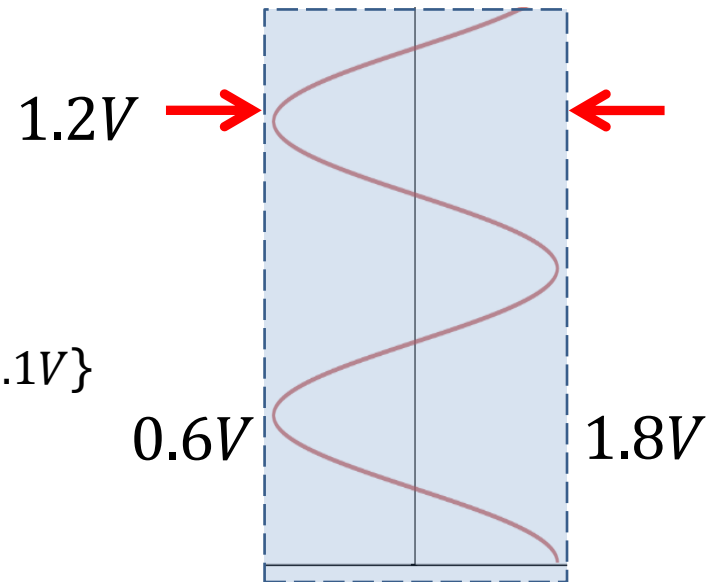


$$V_{IN} = 1.2 + 0.6\cos(2\pi 100t)$$

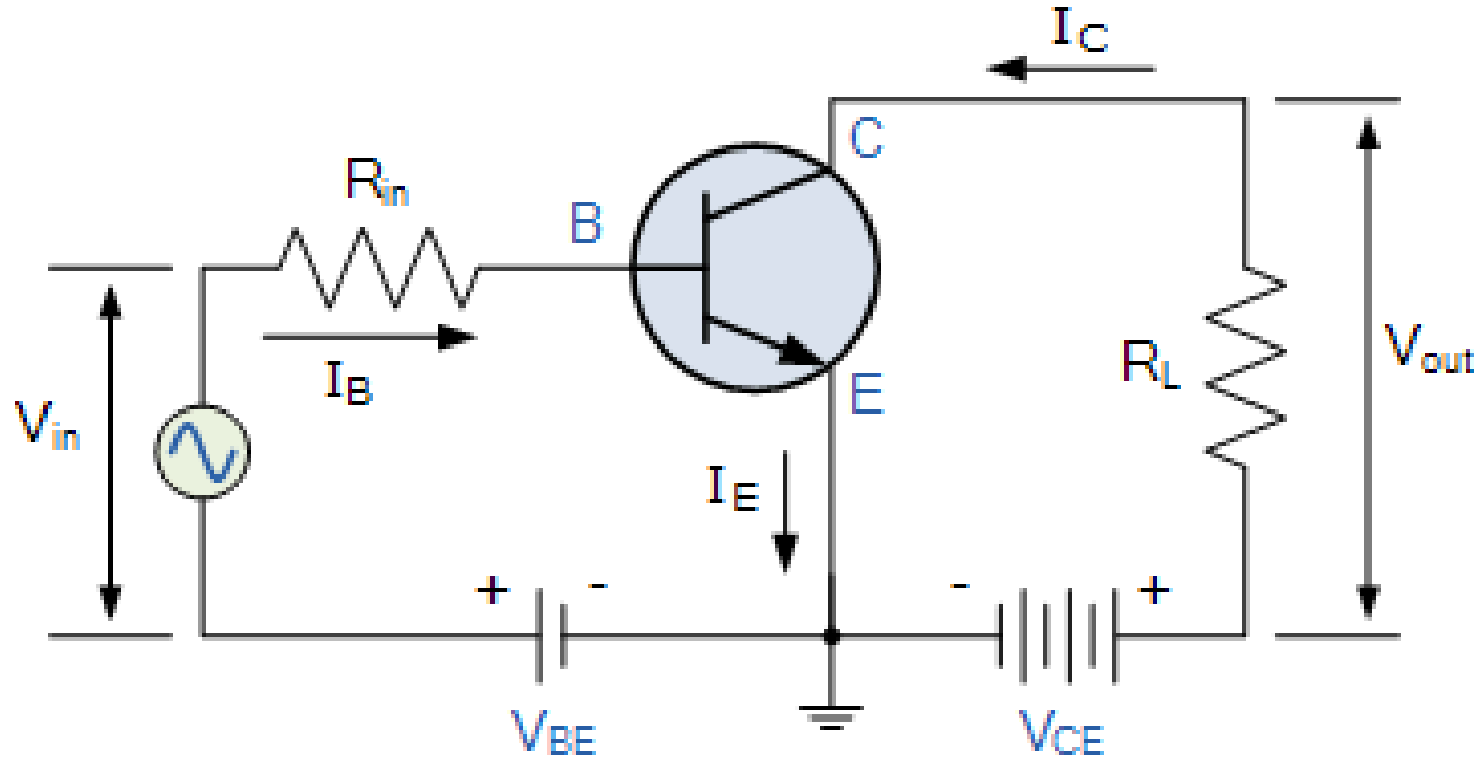
$$V_{OUT} = 2.3 \quad \{V_{in} \leq 0.7V\}$$

$$V_{OUT} = 3.7 - 4.2\cos(2\pi 100t) \quad \{2.3 \geq V_{out} \geq 5.1V\}$$

$$V_{OUT} = 5.1V \quad \{V_{in} \geq 1.7V\}$$



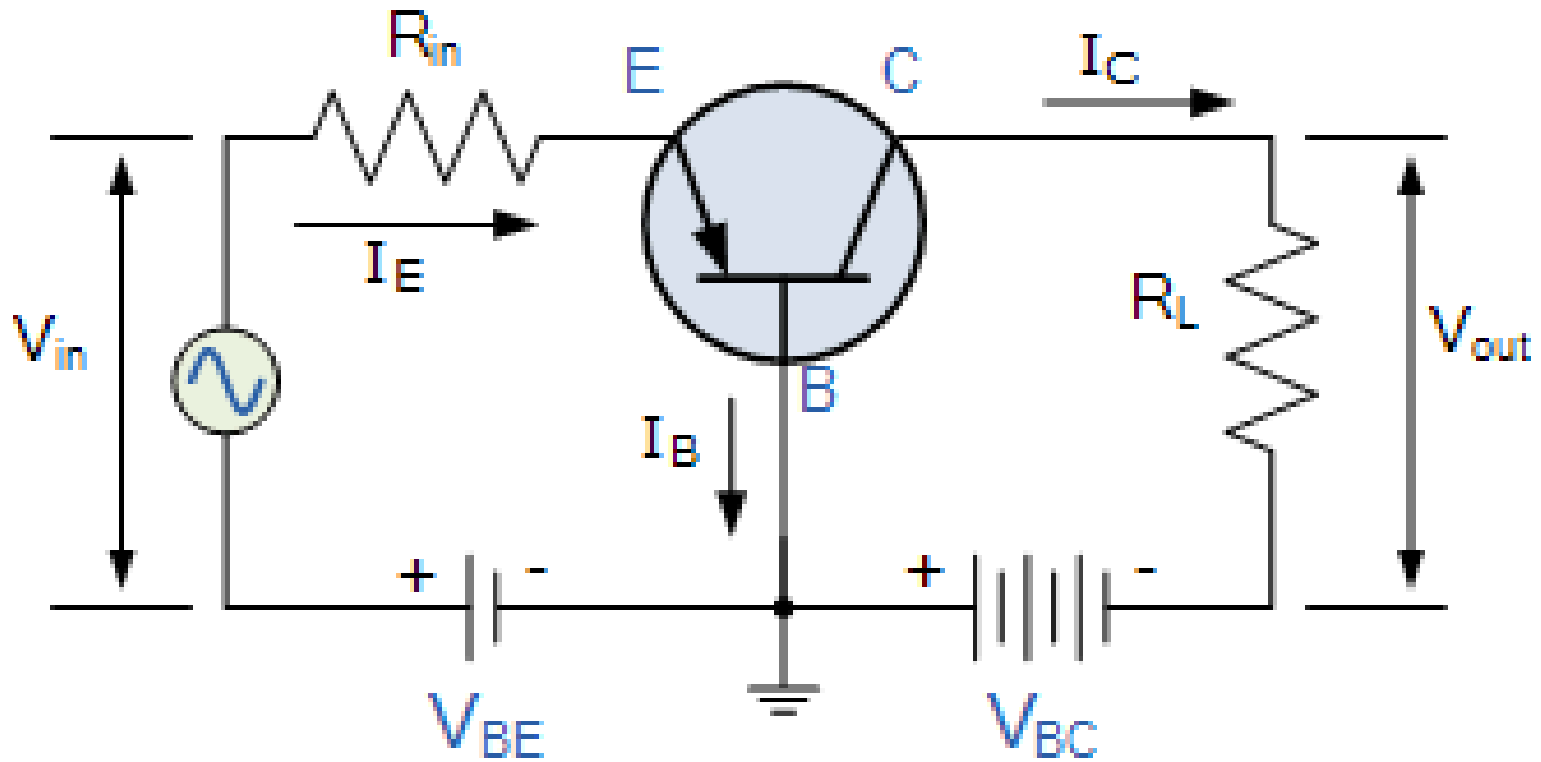
Transistor circuit configurations



Common Emitter

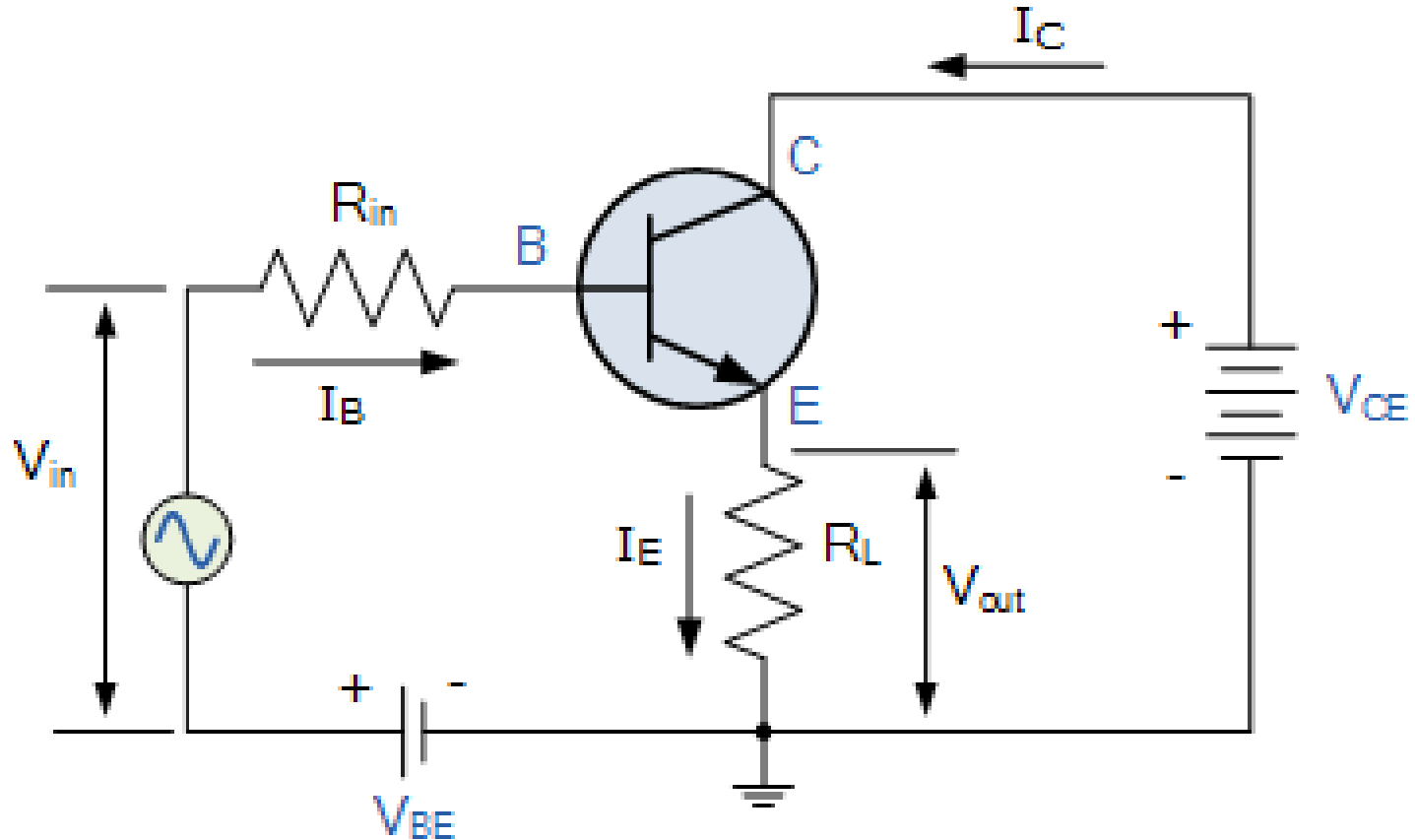
- Current gain
- Voltage gain

Transistor circuit configurations



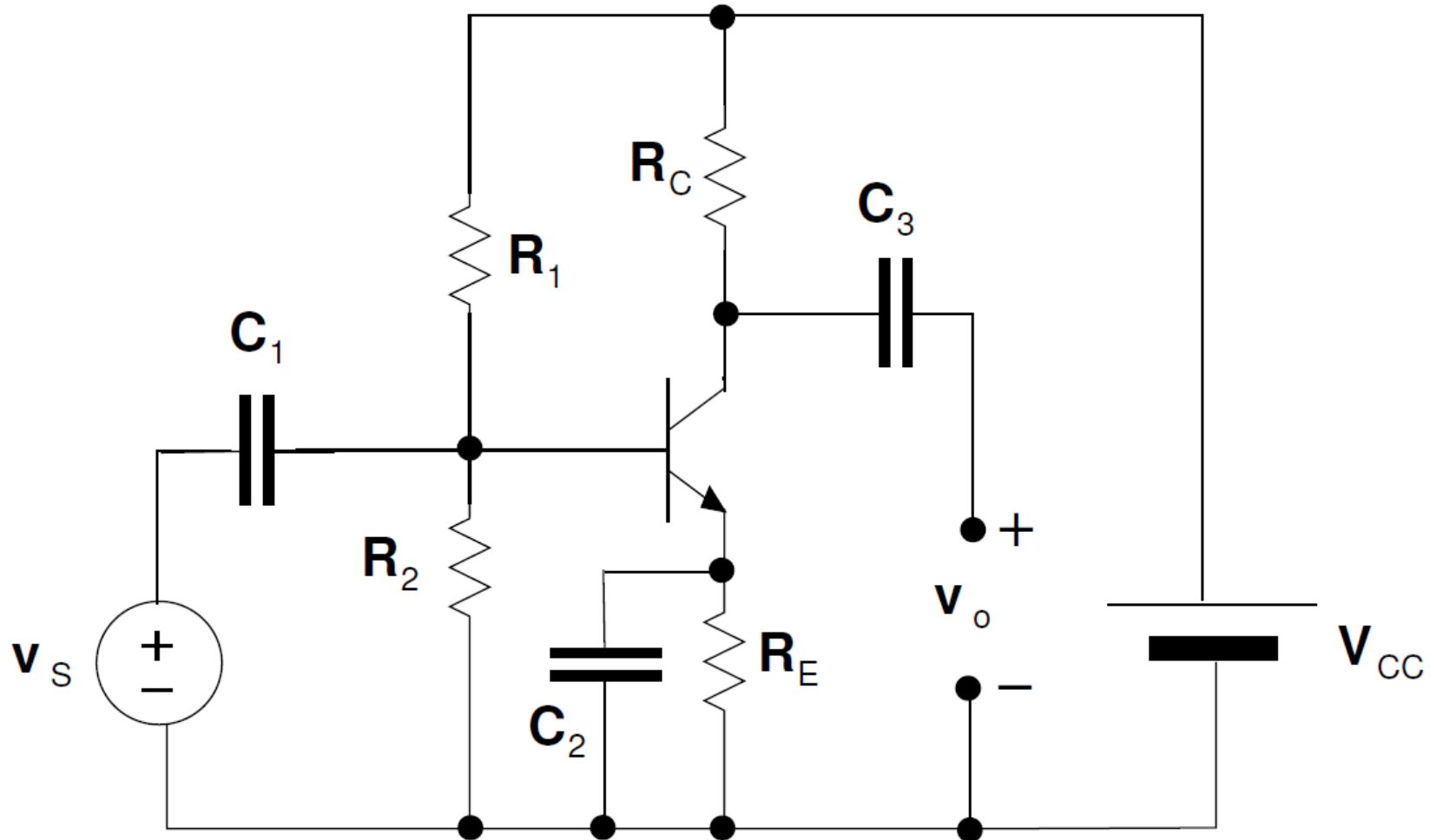
**Common Base
- Voltage gain**

Transistor circuit configurations



**Common Collector
- Current gain**

Common Emitter Amplifier Stage



Small signals equivalent circuit

